

I. Pre-class material Either read the indicated textbook sections OR watch the indicated video.

- (a) **Sections to Read** (All content from Blitzstein and Hwang's *Introduction to Probability* unless otherwise noted). A digital copy of the textbook is available for free via the authors' website.
- Read sections 4.1, 4.2, 4.5
- (b) **Videos to Watch** (All videos from Blitzstein's Math 110 YouTube channel, unless otherwise noted)
- Lecture 9: Expectation, Indicator Random Variables, Linearity (from 14:00 to 41:00)
 - Lecture 10: Expectation Continued (from beginning to 13:00)
 - Read section 4.5 (there isn't a video covering LOTUS in the discrete case)

II. Objectives (By the end of the day's class, students should be able to do the following:)

- State the definition of the expectation of a random variable
- Compute the expectation of the Bernoulli, Binomial, Hypergeometric, and Discrete Uniform random variables using the definition of expectation
- Show that expectation is a linear function of random variables using the definition of expectation
- Use linearity to compute the expectation of Binomial and Hypergeometric random variables
- Use the Law of the Unconscious Statistician (LOTUS) to compute express the expected value of one variable in terms of the pmf of another related variable.

III. Reflection Questions (Submit answers on Gradescope <https://www.gradescope.com/courses/425901>)

- 1) Give an example of two random variables with different distributions that have the same expected value.
- 2) Suppose X is a random variable with expectation $E[X] = \mu$. What is the expectation of the random variable $X - \mu$?
- 3) True or false? If X is a random variable with $E[X] = \mu$, then $E[X^2] = \mu^2$.

IV. Additional Feedback Are there any topics you would like further clarification about? Do you have any additional questions based on the readings / videos? *If not, you may leave this section blank.*